



35 frameworks. For each simulator, the model inputs and outputs are stored in a database. Outputs are  
36 visualized through abacuses, which can be used for virtual practice. MESTRAL modules also include  
37 training exercises and tests to help students to assess the knowledge they have acquired during  
38 consultation of the modules. Finally, MESTRAL has already been successfully tested by different  
39 audiences according to various learning forms.

40

41 **Keywords:** abacus; concept map; electronic knowledge book; food processing; student

42

## 43 1. Introduction

44 Despite an abundant scientific production, the use of models and simulators remains limited  
45 in the food industry where this approach is not familiar, in contrast with other technological sectors,  
46 and there is a clear lack of human resources to adopt modelling approaches in the food industry  
47 (Datta, 2016; Erdogdu et al., 2017; Djekic et al., 2019). Several educational institutions provide  
48 training in computerized techniques and approaches, including mechanistic approaches and multi-  
49 scale modelling, in their food engineering curriculums, to face this issue.

50 Digital resources could contribute to these efforts by implementing simulators as educational  
51 tools in order to prepare future food engineers to use models (Datta, 2016). Among various  
52 initiatives in this sector, a short-term International School on Modelling and Simulation in Food and  
53 Bio Processes (<http://www.virprofood.org/msfs2016/>) was selected to be the training school of the  
54 Cost Action CA15118 FoodMC<sup>1</sup>. Run by the ISEKI<sup>2</sup> Food Association, more than 100 scholars from all  
55 over the world have benefitted from it so far. Another well-known example dedicated to education  
56 in food engineering is the website created by Prof. Paul Singh, which contains video tutorials, lecture  
57 notes, animated films devoted to food processing equipment, virtual experiments, design problems  
58 for what-if analysis, and video lectures based on food science and engineering (Singh, 2008). Prof.  
59 Ashim Datta developed a “learning by doing” approach by introducing modelling and simulation  
60 approaches to solve biological problems, which can be implemented in a food context (Datta, 2015).  
61 In addition to these examples, scientific activity in food engineering generates a great deal of  
62 research products, such as large experimental databases, figures, texts, images and films obtained  
63 with a wide variety of instruments (from images of industrial equipment to microscopic images at  
64 molecular scale), models and simulators, decision-support systems. Most of them are available as  
65 downloadable documents or as web pages on the internet. Many professors individually use their  
66 own research products for teaching purposes. These individual actions could be combined on a  
67 collective scale to convert these research products, including models, into widely available digital  
68 resources.

69 A generic and collaborative approach would contribute to teach modelling in engineering,  
70 and facilitate its appropriation by the students (Carberry & McKenna, 2014). Electronic knowledge  
71 books (eK-book) where knowledge is mainly represented by conceptual maps (Cmaps), might be  
72 used in this purpose. Indeed, they have been shown to be original and effective transfer tools  
73 (Ermine, 2010; Suciu et al., 2012), so they may be converted into digital learning tools. In turn, they  
74 could be shared by educational institutions and made available to a large audience. By providing  
75 **Mathematical and Computer Science Methods for Food Science and Industry Integrating food**

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<sup>1</sup> Mathematical and Computer Science Methods for Food Science and Industry

<sup>2</sup> Integrating food Science and Engineering Knowledge Into the food chain

76 Science and Engineering Knowledge Into the food chain online access, such tools would also offer  
77 good prospects for remote and self-training, and could be used for blended learning, such as in  
78 flipped classrooms (Datta et al., 2020).

79           Given this context, the aim of this article is to present a digital learning tool, to train people  
80 in food processing using models from academia. This tool, organized into a harmonized format using  
81 electronic knowledge books, is named MESTRAL (“Modélisation Et Simulation des TRansformations  
82 ALimentaires” that means in English “Modelling and Simulating Food Processing”). While familiarizing  
83 students with modelling approaches, MESTRAL would, at the same time, encourage their transfer to  
84 industry. For this purpose, we built 15 modules based on eK-book, which are described in the section  
85 2 of this paper. We then implemented simulators based on models for different food processing  
86 applications. These models are detailed in section 3. Finally, after a first validation step involving all  
87 of the authors, we report some of the feedback of a survey taken on the first 100 users.

88

89

## 90 **2. Building the digital learning tool**

### 91 ***2.1 Basic elements of the eK-book***

92           Knowledge transfer is defined here as the addition of transmission, assimilation and eventual  
93 use (Davenport & Prusak, 1998). Knowledge can be collected and represented in various forms, like  
94 concept maps (Cmaps), in an electronic knowledge book (eK-book). To build the eK-book, we  
95 adapted the approach of Ermine (2010), initially designed for capturing know-how for the transfer of  
96 scientific knowledge following a methodology detailed by Suciu et al. (2014). An eK-book is a  
97 hypertext network (Conklin, 1987) in which knowledge is captured in a structured way using Cmaps,  
98 knowledge sheets and a glossary, connected by hypertext links. As a hypermediatool, it makes it  
99 possible to integrate videos, while allowing to download documents and browse web pages from the  
100 internet. As described in greater detail in Section 3, MESTRAL also includes simulators and training  
101 exercises.

102           The canonical concept map (Fig. 1a) is a hierarchical graph that describes a concept according  
103 to four types of ontological relationships: taxonomy (is-a), synonymy (is-synonym), mereology (has-  
104 as-parts) and domain relationship (is-characterized-by, is-measured-by, is-controlled-by, is-  
105 implemented-by, etc.). Taxonomy allows a concept to be positioned in a well-defined group  
106 (Brachman, 1983). Synonymy makes it possible to specify alternative concepts in a given knowledge  
107 domain. Mereology links an entity to its parts (Schulz et al., 2006) through relationships such as  
108 member-collection, matter-object, portion-mass, and phase-activity. Domain relationships make it  
109 possible to indicate how (with which methods) a concept (an operation, a product, a variable, etc.) is  
110 measured, observed, characterized or studied. The application of Cmap in MESTRAL is illustrated by

111 the example taken from the module “Aroma release from yoghurt in mouth” (Fig. 1b). The  
112 specification of the main concept in a Cmap contains other concepts that are directly used to  
113 describe it, such as “strawberry flavour” in the example. This concept is then the main concept of  
114 another Cmap, as symbolized by icons giving access to this next Cmap, via a hyperlink. This way, the  
115 user can navigate within the network of Cmaps. As another example of application to MESTRAL, is  
116 the domain relationship “is characterized by” leading to the concept “viscosity” (of the yoghurt) (Fig.  
117 1b).

118 A knowledge sheet is a document that captures less formal knowledge. It includes eight (8)  
119 fields: *title*, *illustration*, *explanations*, *creation date*, *authors*, *keywords*, *see also* and *literature*  
120 *references*. An example of a knowledge sheet is given for the “aroma release of yoghurt in mouth”  
121 module (Fig. 2). The *illustration* can be a video, a sound, a photo, a drawing, a graph, a table, an  
122 equation, etc., or a link to a document available online. *Explanations* are text that can be formatted  
123 (font, bold, italics, colour, etc.). Each *author* can be clicked on to access their contact details,  
124 including email address and the internet link to the web page of their home laboratory. Each  
125 *keyword*, contained in the glossary of the eK-book, can be clicked on to display its contextualized  
126 definition. The *see also* field contains the links to the related knowledge sheets that provide  
127 additional information. The *literature references* include those cited in the *explanation* field and  
128 other references that provide additional information. They are clickable to open a web page (that of  
129 the article on the publisher's website, for example) or to open a linked document.

130 All the documents in the eK-book and the hypertext links between them constitute a  
131 hypergraph opened on the internet. Thanks to the representation of knowledge, from a general  
132 Cmap to more specific maps, the user can browse the book until the desired detail level is reached.  
133 This knowledge structuring minimizes the disorientation and the cognitive load of the user and thus  
134 promotes the assimilation of knowledge (Amadiou et al., 2009). Disorientation is the property which  
135 assesses the difficulty of the user to locate himself and find information in the eK-book, whereas  
136 cognitive load measures the mental effort invested by the user to grasp the concept maps and to  
137 explore the eK-book.

138

## 139 **2.2 Application to MESTRAL**

140 The cornerstone of any MESTRAL module is the “model Cmap”, which is an instance of the  
141 canonical map (Fig. 1a) specifying the model. It contains all the concepts and information on which  
142 the model relies. Hence, the model Cmap includes the type of model, its hypotheses, its input and  
143 output variables, its implementation, etc (Fig. 3).

144 As for any Cmap, more refined specifications of the concepts are available by clicking on the  
145 icons to open links towards other concept maps or knowledge sheets. The taxonomical relationship

146 “type of model” especially refers to the theoretical framework in which the model is developed. A  
147 sheet, presenting in detail the equations that are solved, can also be opened from the output  
148 variables using the link “is-computed-by”. In addition, the mereology relationship leads to the  
149 hypotheses under which these equations are solved (e.g., the influence of gravity is discarded), and  
150 this box also refers to the assumptions that are made (e.g., the flow is steady at the entrance of the  
151 tubular heat exchanger). Finally, domain relationships refer to the input/output variables of the  
152 model. For example, inputs may be the physical properties of the foods, the equipment geometry or  
153 the process settings. All these concepts may lead to more detailed concepts or knowledge sheets  
154 available by browsing. Outputs also include icons that, once clicked on, open graph sheets where the  
155 variables are represented as functions of input variables (e.g., time -temperature graphs) for selected  
156 values of other inputs. The detailed method of results presentation, i.e., post-processing, is described  
157 in detail in Section 3.3.

158 To complete the eK-book, every MESTRAL module is provided with a glossary where all of the  
159 keywords are listed and defined, and variable units recalled. Input and output variables generally  
160 belong to the keywords list. Their definition appears when browsing the keywords in the text of a  
161 knowledge sheet. In addition, the user looking for a specific keyword can request the list of  
162 documents (Cmap, knowledge sheet) where this keyword appears.

163 At the end of the eK-book, training exercises are proposed with three different levels of  
164 difficulty, beginning with the easiest, which implies knowledge of most basic concepts and of  
165 keyword definition. Conversely, the most difficult ones not only require the acquisition of the  
166 knowledge conveyed by the maps and sheets, but the use of the simulator as well. Simulators are  
167 described in another section. They allow the student to experiment with a “learning by doing”  
168 approach, i.e., virtual practice.

169 At the beginning of every module, six motivating questions are proposed to the student. For  
170 every question, a learning path, or itinerary, has been defined to indicate how to navigate within the  
171 module so as to collect the information required to answer the initial question. These itineraries  
172 make sure that most of the documents can be covered by the student, and they decrease the risk of  
173 disorientation.

174 The eK-book makes it possible to build modules with a common structure, regardless of the  
175 systems studied (food and process), through models that are presented in the next section together  
176 with the simulators implemented.

177

178

### 179 **3. Food processing models in MESTRAL**

#### 180 ***3.1 Various models & frameworks***

181 Many valuable studies have been dedicated to food process modelling and the purpose of  
182 this section is to locate the various approaches used in MESTRAL in the modelling frameworks.  
183 Several reviews have underlined the various potentialities and challenges of modelling and  
184 simulation in food processing (Trystram, 2012; Manlik & Borkar, 2015; Datta, 2016; Saguy, 2016;  
185 Erdogdu et al., 2018; Vitrac & Touffet, 2019). Scientific work in food process engineering has led to  
186 models that use different mathematical formalisms, which can predict the composition (% water,  
187 micronutrients, neo-formed compounds, etc.) and properties (technological, sensory, safety, etc.) of  
188 a product according to its initial composition and the process operating conditions.

189 Computational modelling was developed in food processing, in particular, by applying  
190 Computational Fluid Dynamics and using specialized software (Datta, 2016). This approach, also  
191 referred to as mechanistic, is physics-based and mostly relies on the theoretical framework of  
192 continuum mechanics and thermodynamics. It may appear complex due to mathematical formalism,  
193 and requires considerable investment, first, to analyse the problem and, then, to make the  
194 properties of the food system available. In a complementary manner, experimental approaches may  
195 be guided by statistical models that require the fitting of experimental data according to numerical  
196 procedures and reasoning. This modelling approach can lead to the optimization of a product or a  
197 process in a shorter time, but with lack of flexibility since it is valid in a narrower domain; such  
198 models are data-driven models and include a part of empiricism (Sablani et al., 2007). Note that the  
199 degree of empiricism may be reduced when the model integrates professional know-how with  
200 scientific knowledge, leading to phenomenological models. By doing so, the understanding of the  
201 mechanisms governing the studied phenomena is improved, as illustrated by the basic knowledge  
202 models proposed for the breadmaking chain (Della Valle et al., 2014). Recent approaches at the  
203 crossroads of mathematics and artificial intelligence provide adapted methods to deal with  
204 heterogeneous sources of knowledge and with different mathematical formalisms used by different  
205 disciplines that are manipulated under different forms of uncertainty (natural randomness,  
206 imprecision, data scarcity, vagueness, etc.) (Filter et al., 2015). All these approaches – from  
207 mechanistic to data-driven - represent, in various mathematical forms, the relationships between  
208 input and output variables. They are used in different MESTRAL modules and make it possible to  
209 simulate the food process system in a realistic domain.

210

### 211 **3.2 MESTRAL models**

212 In the following, an overview of the models implemented in MESTRAL is presented, roughly  
213 ordered from a fine to a coarse knowledge grain, and from small to large scales of the system studied  
214 (Fig. 4). The knowledge grain is defined here according to the level of uncertainty of the knowledge  
215 gained by the model results: the larger the uncertainty level, the coarser the grain. The largest

216 systems are at the bottom right and represent a food chain, addressed using the simplest theoretical  
217 framework. As we move along the horizontal axis, the knowledge grain becomes coarser and the  
218 model predictions become more uncertain, resulting in general trends rather than accurate  
219 predictions. In Fig. 4, the overall trend suggests that MESTRAL models arrange around the bisector.  
220 However, it is noteworthy that food engineering models may lead to acceptable precision (i.e. a fine  
221 knowledge grain) at a large scale, by computing properties from knowledge about structure at a  
222 lower scale, which is precisely the challenge addressed by multi-scale modelling (Ho et al., 2013).

223 As seen for the complementary information reported in Table 1, these models rely on  
224 different theoretical frameworks, from continuum mechanics (physics-based models) to stochastic  
225 approaches and statistical analysis (data-driven models). They are implemented through various  
226 numerical and computer resources, either based on commercial software, possibly using Finite  
227 Elements (FE), or developed by the scientists themselves. For the purpose of simplicity, the literature  
228 references that have led to the development and validation of every model are not mentioned all,  
229 but the most recent ones are quoted so that the reader may, in turn, find more in-depth information  
230 when needed.

231 Deep fat frying of starch foods involves coupled heat and mass (water and oil) internal  
232 transfers. By solving the partial differential equations (PDE) of these transfers in thin or thick slices of  
233 plantain banana, the 2D numerical, FE-based model makes it possible to predict the nutritional  
234 impact through various indicators (nutrient density and toxic components such as acrylamide) that  
235 are linked to computed fields such as temperature, moisture and oil content (Bassama et al., 2015).

236 Using the same formulation and numerical resources to solve heat mass transfer PDEs, a  
237 deterministic approach is proposed to predict the transformation of starch suspensions in a tubular  
238 heat exchanger by computing the fields of velocity, pressure and temperature along the tube. In this  
239 case, an essential original feature comes from the two-way coupling of rheology, fluid flow and heat  
240 transfer, taken into account by the kinetics of starch granule swelling, which depends on  
241 temperature and drastically modifies the apparent viscosity (Plana-Fattori et al., 2016).

242 Based on the solution of the mass balance equations in three compartments  
243 (nose/pharynx/food layer), the model of *in vivo* aroma release computes the evolution of the  
244 concentrations of representative aroma compounds (diacetyl and ethyl octanoate). The evolution of  
245 concentrations is computed in the product and in the air after swallowing for yoghurts with various  
246 fat contents (Trelea et al., 2008). Because it integrates the consumer's physiology and because aroma  
247 release is correlated with sensory perception, this model is used to address the re-engineering of  
248 food formulations.

249 Solid food texture is addressed by a 3D numerical, FE-based mechanical model that considers  
250 cereal food as a solid foam in the linear elastic domain. Compression loading of virtual realistic



251 cellular structures is simulated and the model computes the variations of foam stiffness, represented  
252 by the mechanical property of Young's modulus with respect to the foam density. The correlation  
253 between foam density and stiffness is compared to the analytical solution from Gibson-Ashby's  
254 model, and with experimental data obtained on bread, biscuits and breakfast cereals (Guessasma et  
255 al., 2008).

256 Non-conventional heating is treated through a simplified 1D numerical Finite Volume model  
257 that accounts for microwave-matter interactions in the case of unidirectional propagation (plane  
258 wave) (Curet et al., 2009). The model provides a tool for predicting temperature kinetics during a  
259 microwave heat treatment, as well as the absorbed power density as a function of the depth for two  
260 foods - bread and meat - to deal with two different moisture levels.

261 The modelling of dairy food foaming considers the 1D-flow of viscous fluid in a static mixer  
262 (SMX™) and its expansion tube, where the pressure drop is computed at various steps (Laporte et al.,  
263 2014). Hence, along the tube, it is possible to calculate the incorporated air fraction and size of the  
264 bubbles and the power consumption from geometry data, gas and liquid flow rates, as well as the  
265 rheological properties of the dairy formulation.

266 The flow of molten starchy products in a twin screw extruder is modelled in the same way by  
267 summing the pressure drop or rise in each screw part (Della Valle et al., 1993). This analytically  
268 solved, 1D model makes it possible to compute the main flow variables, melt temperature, pressure,  
269 shear rate and viscosity, and the specific mechanical energy along the screws. The model is  
270 implemented in a commercial software program called Ludovic®, that is used to perform simulations.  
271 Expansion of the starch melt at the die outlet to generate airy snack foods has also been tackled by a  
272 phenomenological model that predicts cellular structure (Kristiawan et al., 2019).

273 The model of food packaging is based on ordinary differential equations (ODEs) that describe  
274 mass transfer phenomena in the system defined by the food and the packaging material (Guillard et  
275 al., 2012). By coupling these ODEs with the gas consumption of microbial species, it makes it possible  
276 to predict product shelf life (Chaix et al., 2015). It also includes a multi-criteria decision support  
277 system that helps the user to choose a package for a given food. The multi-criteria choice is then  
278 adapted to the different actors in the food packaging sector (Guillard et al., 2015).

279 The model of the hot air-drying process of agricultural products (corn and rice grains) is  
280 based on the concept of drying kinetics, which explicitly considers the heat and mass transfers  
281 between three compartments: the surrounding air, and the external layer and the core of the grain  
282 (Abud Archila et al., 2000). In addition to time-temperature and moisture variations, the model also  
283 predicts the impact of drying on grain quality using an image bank.

284 Similar phenomena of heat and matter transfer applied to the cooling of carcasses can be  
285 modelled using a 1D numerical approach (Kondjoyan & Daudin, 1997) that makes it possible to

286 calculate the kinetics of temperature at different points (surface, core, average) of the carcass for  
287 two animal sizes (typically pork and rabbit). The evolution of weight loss of the carcass is also  
288 predicted, keeping in mind that this loss must be minimized for quality purposes.

289         Still considering fresh animal proteins (white fish and beef), an application of the high-  
290 pressure (HP) treatment process (up to 500 MPa) is addressed through the use of experimental  
291 results (Cheret et al., 2005). In this case, the phenomenological model makes it possible to study the  
292 increase in the shelf life of these products thanks to this HP process, and its parameters (time,  
293 pressure level), while taking the organoleptic changes (texture and colour) observed after treatment  
294 into account.

295         The mixing process in a stirred tank is addressed by modelling principles that use dimensional  
296 analysis, with applications to the homogenization of sucrose solutions, the dissolution of dairy  
297 powders and heat transfer within viscous solutions of glucose syrup. It is then possible to predict the  
298 mixing time and the power demand of the equipment, the dissolving time and the heat transfer  
299 coefficient using abacuses of dimensionless numbers (Reynolds, Nusselt and power numbers),  
300 established from the analysis of the mixing operation and from dedicated experiments (Delaplace et  
301 al., 2015). In this case, the interest of using dimensionless numbers to reason about scaling up using  
302 a physics-based approach is shown.

303         The mixing process is also a critical operation in the bread-making chain since it converts a  
304 solid divided medium, the flour, into a continuous viscoelastic one, the dough. In this case, mixing  
305 modelling is addressed through an expert system known as AsCoPain<sup>®</sup>, which models the bread  
306 technologists' expertise using a qualitative algebra (Ndiaye et al., 2009). This model makes it possible  
307 to calculate the sensory variables that define the state of the bread dough on the basis of the  
308 formulation variables (characteristics of the flour) and the operating conditions of the mixer (Kansou  
309 et al., 2014). This module also includes a simple phenomenological model of the dough-proofing  
310 stage, directly affected by parameters of the mixing process (Kansou et al., 2013).

311         Heterogeneous knowledge can also be assembled in a model using Dynamic Bayesian  
312 Networks (DBN) in order to predict the ripening process of Camembert-type cheese (Baudrit et al.,  
313 2010). While also introducing conditional probabilities, the model maps the evolution of the  
314 organoleptic properties of cheese according to microbial activity, which itself depends on its  
315 environment. The model helps to reduce the uncertainties linked to the working, the design and the  
316 control of the ripening process.

317         Conditional probabilities are also used for predictive microbiology, which is coupled to a  
318 simple heat transfer model of three compartments of the cold chain. This model describes the  
319 evolution of the temperature and of the microbial load of ham slices (Flick et al., 2012). Taking  
320 several random variables into account (residence time in the different compartments, adjustment of

321 the thermostat of the refrigerator, speed of growth of micro-organisms), the model makes it possible  
322 to represent the influence of equipment and consumer behaviour on the health safety aspects of the  
323 ham slices.

324 As may be seen from this rapid review, these models address a large panel of real (food and  
325 process) systems, at various scales and through different theoretical frameworks (Fig. 4). Actual  
326 access to MESTRAL on the computer screen is given by the portal presenting the fifteen (15)  
327 modules, each one illustrated by an image of the system, according to following link  
328 <http://thot.i2m.u-bordeaux.fr/mestral/portail/>. Each model is assigned a model Cmap (see Section  
329 2.2) and a simulator that is embedded in the modules as described below.

330

### 331 ***3.3 Post-processing and simulators***

332 Implementing MESTRAL models raises two issues: first, the access to commercial modelling  
333 software; and, second, the necessity of having sufficient computation resources to run the  
334 simulation. Both are of course prohibitive for a potentially intense use of the simulators by the  
335 students, exacerbated by remote access from home and the use of their own terminals (smartphone,  
336 tablet or PC). Therefore, a database was included in each module by collecting the results of output  
337 variables (values computed by the model) for a selected number of values of input variables. This  
338 database is run using abacuses, a technique traditionally used for learning purposes, as suggested by  
339 Lopez et al. (2018) for mechanical material engineering. Clearly, the representation of abacuses is  
340 limited by the large number of variables and of the values that these variables can take. In MESTRAL,  
341 no more than four to five abacuses, one per output variable, with four to five curves, are presented  
342 on the same screen page (Fig. 5a, b). Sliders make it possible to select discrete values (up to ten  
343 values) of the input variables. For every combination of sliders positions, a set of graphs is  
344 instantaneously presented. In Fig. 5a, graphs represent, for example, the grain water content after  
345 various drying times and for different drying conditions. In Fig. 5b, the graphs represent the  
346 variations of starchy product temperature, pressure, viscosity at the extruder die outlet, and specific  
347 mechanical energy for various screw speed, feed rate and barrel temperature values.

348 The simulator includes the abacuses drawn from the database and the graphical  
349 representation of the results. All simulator interfaces are developed in HTML5, CSS3 and Javascript.  
350 These are the core technologies for building web pages, which allows the simulators to be easily  
351 accessible in the future. Hence, the generation of abacuses is automated and their presentation is  
352 adapted to the student using digital charts that allow storage and post-processing of highly variable  
353 solutions in a very efficient way (Lopez et al., 2018). Note that it allows any user to perform a  
354 simulation of the process without fully understanding the theoretical framework of the model, but  
355 with knowledge of its basic principles. Conversely, it can incite the student to become acquainted

356 with this framework as well as with the equations on which it is based, since this ease-of-use can be  
357 compared to the possibility of “driving a car without knowing how its engine works”.

358

359

#### 360 **4. First tests and surveys for validation**

361 The validation of the work involved two testing steps corresponding to two different  
362 audiences and questionnaires.

363 In the first one, performed during a two-day seminar, the twenty-five (25) contributors first  
364 checked the consistency, the completeness and the accuracy of the content of their module. They  
365 also acted as “beta-testers” by browsing two to three other modules for 2 to 4 hours each. To do  
366 this, they had to fill in an open questionnaire (see Appendix A), and declare whether they considered  
367 themselves as expert or novice in the field covered by the module. Those who have already worked  
368 and published in the area are referred to as experts, whereas those who have never read any  
369 scientific article on the topic are considered as novice. The answers were collated and transmitted to  
370 each of the contributors who then performed the appropriate corrections.

371 In a second step, MESTRAL was tested by a large audience (100 users) from various horizons,  
372 students and professionals, and with various education levels in engineering and science (chemical,  
373 agricultural), from bachelor’s degrees to PhDs, on a volunteer and anonymous basis. It took place  
374 during the period from September 2018 to April 2019. No specific instruction was given and testers  
375 could choose any module on the website “<http://thot.i2m.u-bordeaux.fr/mestral/portail/>” using  
376 appropriate identifier and password. So MESTRAL was mainly tested for self-learning, possibly  
377 leading to a flipped classroom. Conversely, in some cases, blended learning conditions were also  
378 proposed. In this case, the students were asked to use a module in the presence of the teacher, who  
379 was the module’s contributor. After each test, the user was asked to fill in a questionnaire (see  
380 Appendix B) of twenty (20) questions. The results reported in Fig. 6 show that: (a) more than 90% of  
381 the testers were (quite) satisfied overall and (b) found the content clear and relevant; (c) the learning  
382 effort was judged moderate and equally distributed from significant to very low; whereas (d) about  
383 75% found browsing on the eK-book quite easy. Finally, a large majority found it easier to learn about  
384 the models by running the simulators than by a traditional presentation of the model equations and  
385 of the theoretical framework (Fig. 6e).

386 However, this positive trend should be balanced by the necessity to test the students for the  
387 acquired knowledge, a purpose for which learning tests (quizzes) have also been planned and  
388 implemented. The aim of this survey was clearly not to obtain definitive answers, but just to obtain  
389 initial feedback about the way the knowledge, and especially the models, are presented in the eK-  
390 book. Altogether, the 15 MESTRAL modules integrated in the eK-book contain over six hundred (600)

391 Cmaps and more than seven hundred (700) knowledge sheets, which leads to an overall total of  
392 approximately 150 h of teaching, including student's effort. A more systematic evaluation by a larger  
393 group of students is to be scheduled under well-defined learning conditions. From the feedback, the  
394 necessary improvements will be performed prior to delivering this digital resource to educational  
395 institutions. Up until now, all of the modules were written in French, and one has been translated  
396 into English (Aroma release from yoghurt in mouth), which suggests that translation into another  
397 language is within reach, provided the necessary resources are available. Presently, free access to  
398 MESTRAL may be granted upon personal request to the corresponding author of this paper.

399

## 400 **5. Conclusion**

401 In this paper, we have presented an original digital learning tool known as MESTRAL. It was  
402 built for the purpose of teaching food processing using models and that covers approximately 150 h  
403 of teaching, including student's effort. It is based on knowledge engineering methods such as  
404 concept maps, which have been adapted for this purpose, and are implemented in an electronic  
405 knowledge book. Fifteen (15) models, all derived from research studies, are treated. They cover a  
406 wide range of real applications and can be mapped according to the system scale and the knowledge  
407 grain assessed by the different theoretical frameworks under which they are developed. This variety  
408 may clearly be a source of complexity for the student. However, cognitive load and disorientation can  
409 be reduced as a result of the harmonized knowledge representation. Furthermore, using the abacus  
410 technique, the results of simulations integrated into a database are graphically represented. Hence,  
411 the user can simulate various operations of the modelled system and test the influence of changes of  
412 either process conditions or product formulation on final food properties and process performances.  
413 Finally, an initial validation test on a large audience made it possible to obtain encouraging feedback.  
414 As advocated by the basic hypothesis of this work, this result suggests that by letting students  
415 simulate the workings of the (food and process) system, such a tool may contribute to sensitizing  
416 them about modelling approaches and various theoretical frameworks. Furthermore, since the  
417 results are derived from recent scientific research studies, they may draw the student's attention to  
418 innovative processes. As a digital learning tool, MESTRAL could provide students with remote and  
419 self-training resources, and could also be used for blended learning by educational institutions.  
420 Finally, because of its potential to share digital resources, it contributes to a collaborative response  
421 to the teaching of modelling and favours the transfer of computer-aided engineering to the food  
422 industry.

423

424

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431

432

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549

550 **List of figures**

551

552 **Figure 1:** The canonical concept map (a) and an example of an application taken from the module  
553 “Aroma release from yoghurt in mouth” (b). Concepts are written in the boxes. They are linked by  
554 relationships from left to right: taxonomy (pink), synonymy (grey), mereology (blue) and domain  
555 (green). In the example, there is no synonymy relationship. Only the taxonomic relationship is always  
556 present on all the instances of the canonical concept map. Small icons that appear in Cmap (b) give  
557 access to another Cmap or to a knowledge sheet that can be opened by clicking on it.

558

559 **Figure 2:** Example of a knowledge sheet taken from the module “Aroma release from yoghurt in  
560 mouth” with the eight fields, from top to bottom: *title, illustration, explanations, creation date,*  
561 *authors, keywords, see also and literature references.*

562

563 **Figure 3:** Concept map adapted to the representation of the model, taking the model of “Heat  
564 exchanger for starch suspension”, for example. Note that a concept “simulator” is added on the right  
565 to represent how the model is implemented and to give access to the results computed by the  
566 model. A knowledge sheet may be opened from this Cmap using the icons, providing information  
567 about the theoretical framework on which the model is based.

568

569 **Figure 4:** Schematic mapping of the various models implemented in MESTRAL according to their  
570 knowledge grain (from more to less accurate predictions, x axis) and size scale of the modelled  
571 system (y axis). Models dealing with multiphase transport of heat and mass in (semi) solid medium  
572 are coded in red, whereas blue ones refer more to models that address the flow of complex media,  
573 with momentum transfer and large deformations, i.e., where rheology is pivotal. Purple codes stand  
574 for models involving both.

575

576 **Figure 5:** Two screenshots of the MESTRAL simulator for “rice grain drying” (a) and “extrusion-  
577 cooking of cereals” (b). On the upper part, sliders (green) feature the numerical values of model  
578 input variables. Below, several abacuses present the simulation results for the above input  
579 combinations and for various model parameters (initial and drying conditions in the case of grain  
580 drying (a); extruder operating conditions in the case of extrusion (b). Note that for real use, the  
581 graphs may be enlarged at the user’s demand.

582

583 **Figure 6:** Overview of the results of the second validation step, i.e., testing MESTRAL on a large  
584 audience (100 students) on the basis of a questionnaire (Appendix B): (a) overall satisfaction

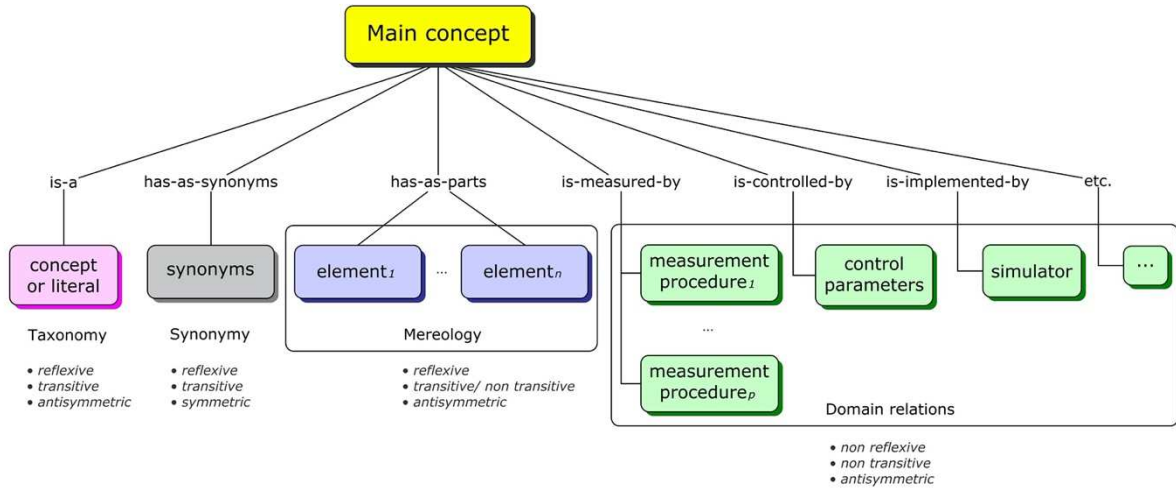
585 (question #9); (b) relevance and clarity of the knowledge conveyed; (c) mental effort made (cognitive  
586 load, #12); (d) navigating smoothness (#14); and (e) comparison to conventional lesson (#17).

587

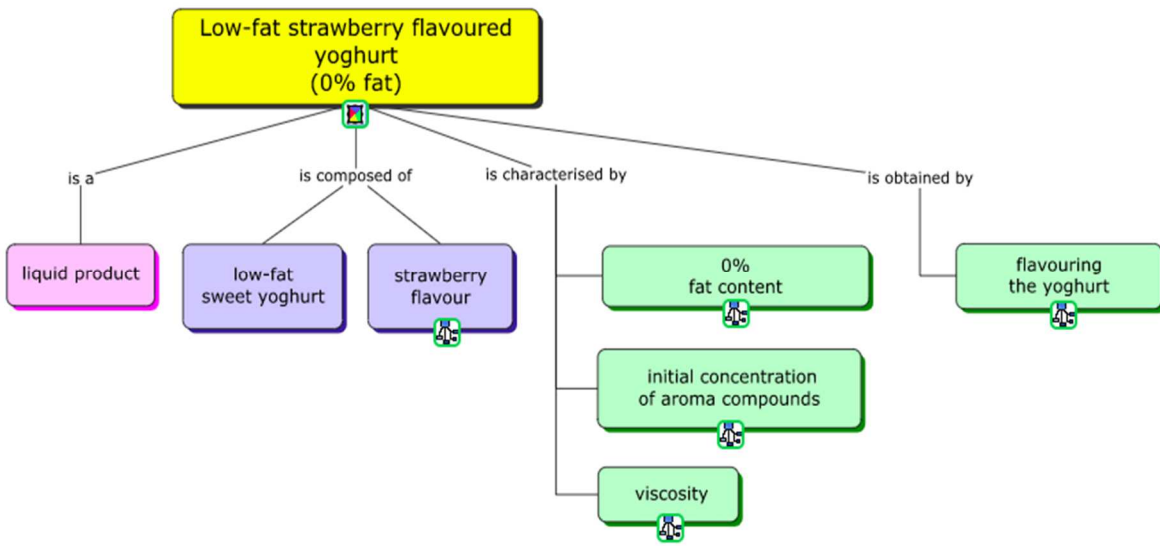
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(a)



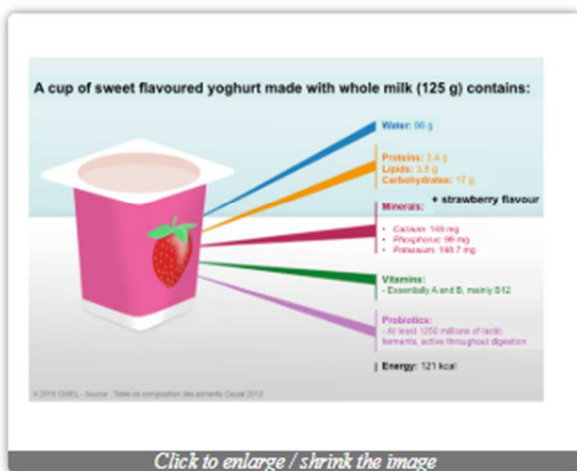
(b)



MESTRAL

Fig.1

## Studied product: strawberry flavoured yoghurt



A flavoured yoghurt is a widely-consumed product, essentially composed of milk, lactic ferments (or lactic acid bacteria) and sugars to which flavour is added. It has a wide range of texture and rheological properties, depending on the content of proteins, fat and how it has been manufactured.

Source : CNIEL (2015)

Author(s) [Violaine Athès](#) [Ioan Cristian Trelea](#) [Ioana Suci](#) [Hélène Etienne](#)

Keywords [ [flavour](#) ] [ [aroma compound](#) ] [ [matrix \(or food product\)](#) ] [ [strawberry flavoured yoghurt](#) ]

#### See Also

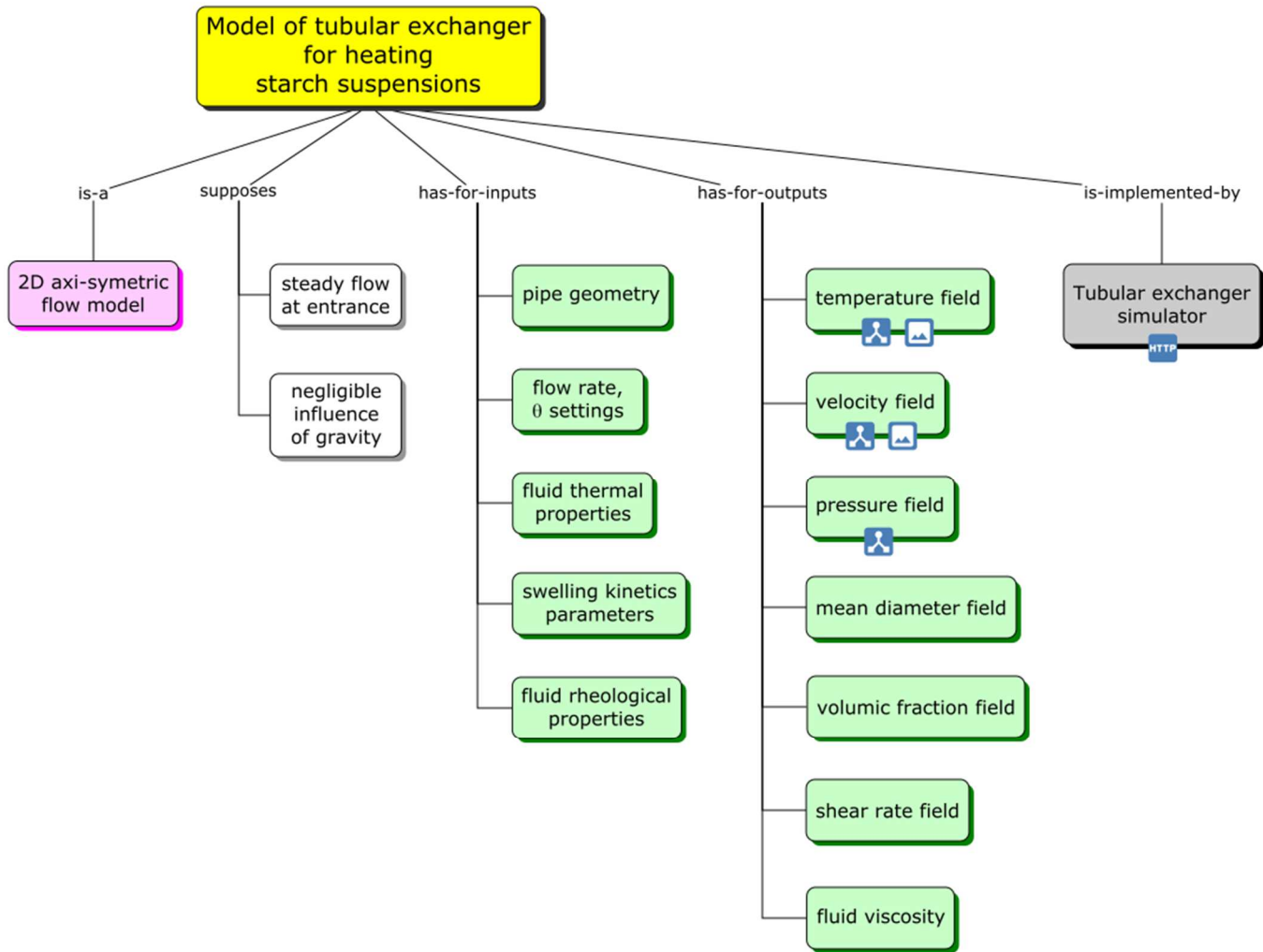
[The aroma compounds of the strawberry flavour](#)  
[The key issues in the aromatic formulation of low-fat yoghurts](#)

#### References

CNIEL (2015) Table de composition des aliments Ciquel

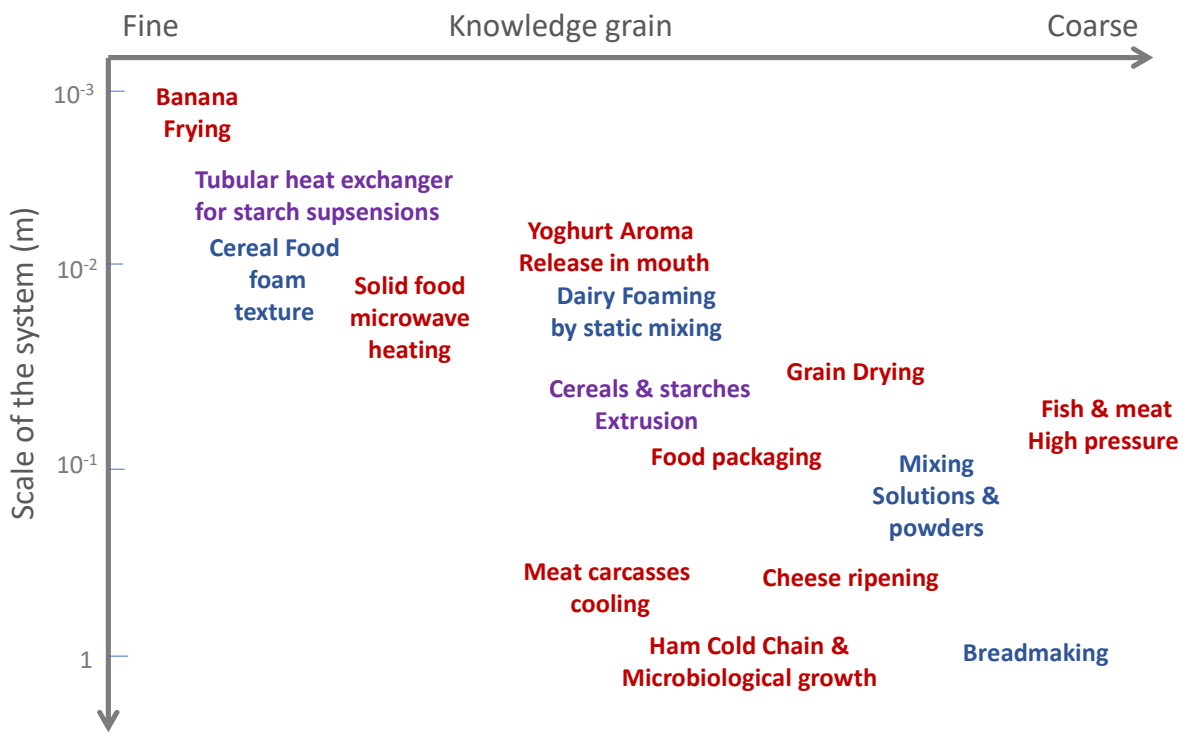


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Mestral

Fig.3.

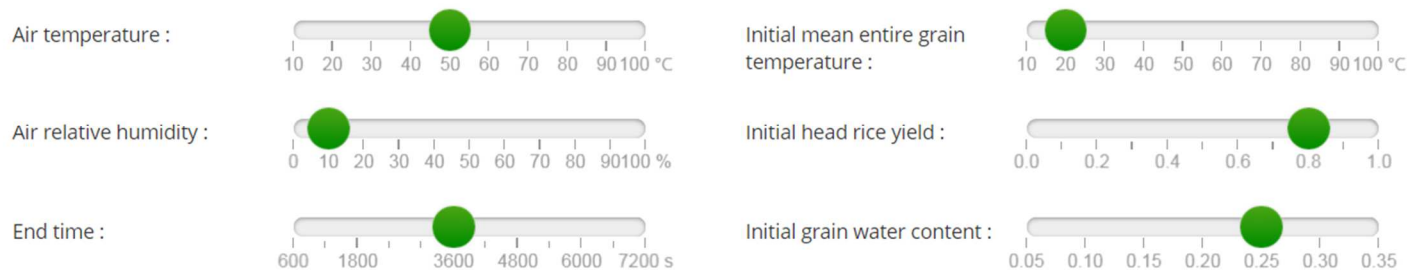


MESTRAL

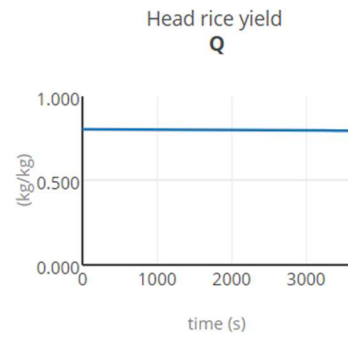
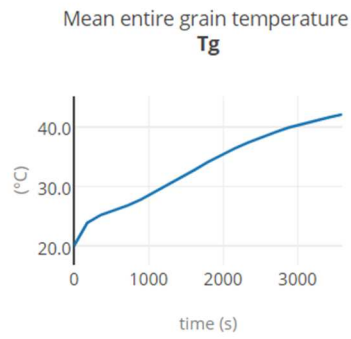
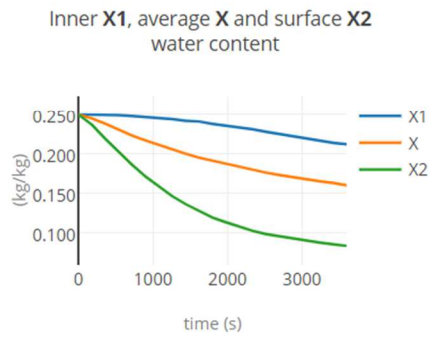
Fig. 4

(a)

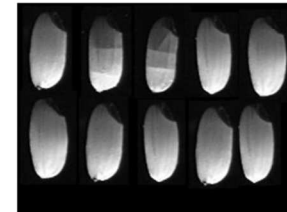
### AgreenCamp - MESTRAL : Simulator of Rice grain drying



Standard values Automatic setting  Display results



Rice final grain quality (head rice yield)  $Q_f \approx 0.791$  illustrated by :



Print this page



(b)

## AgreenCamp - MESTRAL : Simulator of extrusion-cooking of cereals and starchy products

Amylose content (%) :



Length of reverse screw element :



Water content (%) :



Die diameter :

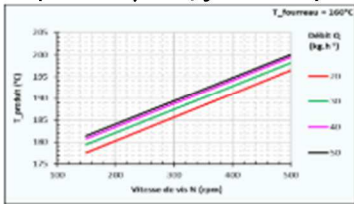


Standard values

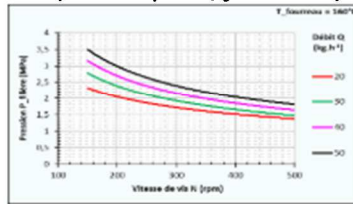
Automatic setting

Display results

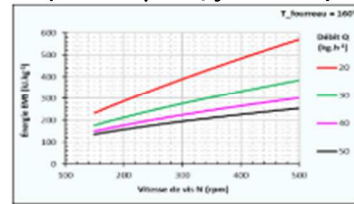
*T<sub>product</sub>*  
(screw speed, feed rate)



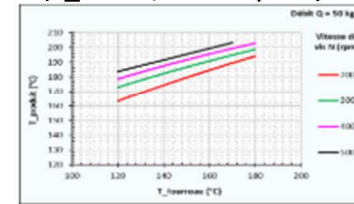
*Pressure<sub>product</sub>*  
(screw speed, feed rate)



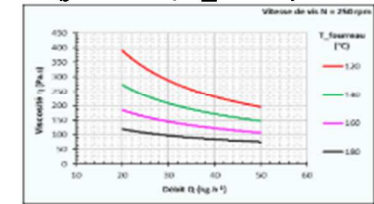
*SME*  
(screw speed, feed rate)



*T<sub>product</sub>*  
(T<sub>Barrel</sub>, screw speed)



*Viscosity<sub>product</sub>*  
(feed rate, T<sub>Barrel</sub>)



Please click on the graphs to enlarge.

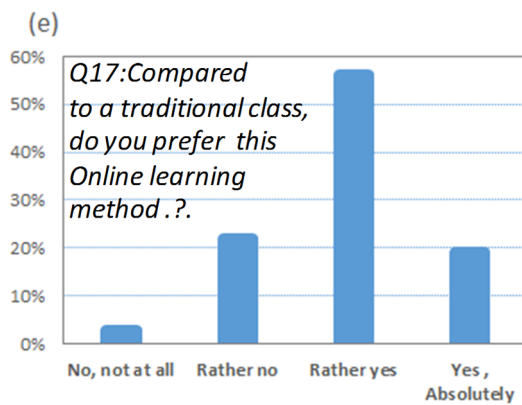
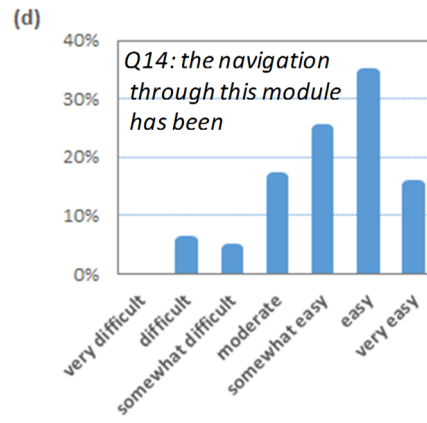
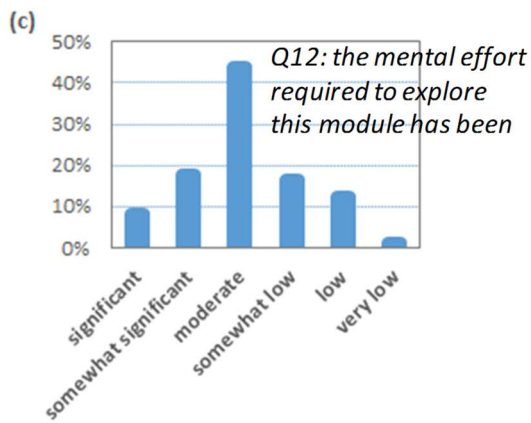
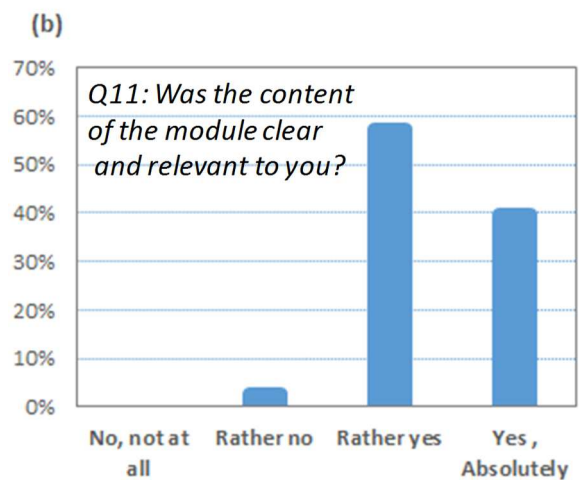
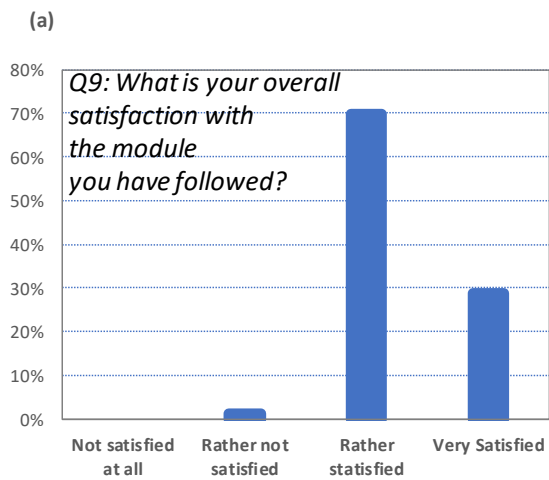
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MESTRAL

Fig.5



**Table 1:** Overview of the different models represented in MESTRAL and their main characteristics (FEM=Finite Element Method) ordered according to increasing system scale length and coarseness of knowledge grain. « Analytical with compartment » means that differential equations of heat, or mass, or momentum are solved explicitly, (time or space) step by step.

Title & Process	Food system	Theoretical framework and model type	Inputs <sup>a</sup>	Outputs <sup>a</sup>	Simulator basis	Reference
Frying	Banana	2D-Numerical (FEM)	Product thermal properties and geometry, oil properties and fryer settings	Fields of water, oil contents and temperature ; composition, micronutrients and nutrition indices	Comsol <sup>b</sup>	Bassama et al., (2015)
Tubular heat exchanger	Starch suspension	2D- Numerical (FEM)	Exchanger geometry & settings, suspension thermo-rheological properties and starch swelling kinetics	Fields of temperature, velocity, pressure, granule diameter and volume fraction	Comsol <sup>b</sup>	Plana-Fattori et al., (2016)
Aroma release	Yoghurt in mouth	Numerical with compartments	Food composition, transfer and partition coefficients, consumer's physiology	Time-concentration of aroma compounds in nose, pharynx and product	MATLAB <sup>®</sup>	Trelea et al., (2008)
Texture	Cereal solid foams	3D Numerical (FEM)	Food sample geometry, cellular structure and cell wall's Young moduli	Local stress & strain fields, foam Young modulus	Comsol <sup>b</sup>	Guessasma et al., (2008)
Microwave heating	Pan bread, beef meat	1D Numerical (Finite Volume)	Product physical properties and thickness, microwave operating conditions	Time –temperature and microwave absorbed power at different locations in food	MATLAB <sup>®</sup>	Curet et al., (2009)
Static mixer	Milk liquid foams	Analytical with Compartments	Fluid properties, mixer geometry and settings	Pressure profile, air volume fraction, mean bubble diameter, foam viscosity	Personal <sup>c</sup>	Laporte et al., (2014)
Extrusion cooking	Cereals & starchy products	Analytical with Compartments	Material thermo-rheological properties, extruder geometry and settings	Material pressure, temperature, residence time, viscosity and specific energy profiles	Ludovic <sup>®</sup>	Della Valle et al., (1993)

Packaging	Dry foods , or fresh respiring or not	Analytical with Compartment and 1D-numerical	Food & packaging physical propertie and geometry, storage conditions	Head space CO <sub>2</sub> , O <sub>2</sub> and micro-organisms time variations. Packaging material selection	Personal <sup>c</sup>	Guillard et al., Chaix et al. (2015)
Drying	Corn and rice grains	Analytical with Compartment	Inner and surface initial moisture content, grain physical properties and dryer settings	Time variations of grain temperature, moisture content & quality	Personal <sup>c</sup>	Abud Archila et al., (2000)
Cooling	Meat (pork, rabbit) carcass	1D - Numerical	Size, mass & physical properties of carcass, conditions of air velocity, humidity, temperature & turbulence	Time -temperature & water mass loss at surface, and inside variations	Personal <sup>c</sup>	Kondjoyan & Daudin, (1997)
High pressure	Fish and meat	Phenomenological	Initial products characteristics & composition, time, pressure & temperature settings	Final microbial load, texture and color	Personal <sup>c</sup>	Cheret et al., (2005)
Agitation	Syrups and milk powders	Dimensional analysis	Geometry, mixer settings, product properties	Homogenisation or dissolution times, consumed power	Personal <sup>c</sup>	Delaplace et al., (2015)
Bread making	Wheat flour dough	Qualitative algebrae and phenomenological	Flour composition, mixer settings, proofing time	Dough rheological properties, porosity and stability after proofing	AsCoPain <sup>®</sup>	Ndiaye et al., (2009)
Ripening	Cheese	Dynamic Bayesian network	Initial pH temperature, composition, ripening time	Microbial behaviour and evolution of sensory properties	Personal <sup>c</sup>	Baudrit et al., (2010)
Cold chain and micro-biological growth	Ham	Analytical with heat transfer coupled to previsional microbiology	probability distributions of residence time, ambient temperature, microbial growth	product temperature and microbial load evolutions	Personal <sup>c</sup>	Flick et al., (2012)

<sup>a</sup> these characteristics are not exhaustive of the model considered but they provide more insight on the system (process, food) modelled.

<sup>b</sup> Comsol stands for COMSOL Multiphysics<sup>®</sup>

<sup>c</sup> « Personal » means that the model has been implemented by the author through current software resources (Office or else)