Electrical resistivity monitoring of a SiC/[Si-B-C] composite under oxidizing environments

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Abstract. The introduction of Ceramic Matrix Composites parts in civil aeronautics requires a thorough understanding of their evolution under the oxidizing environments present within the engines. In this respect, a SiC_f/PyC/[Si-B-C]_m material has been tested in fatigue at 450°C and 100 MPa (which is a typical stress during take-off) under two types of environmental conditions: ambient air, and moist air with an imposed water pressure of 10 kPa. Static fatigue and cyclic fatigue at a frequency of 1 Hz were both performed with these two conditions. As expected, the additional presence of moisture contributes to increase the degradation of the mechanical properties of the material, leading to shorter lifetimes and higher increases in electrical resistivity. It is shown that the pyrocarbon interphases are the main electrical conductors in this material: the electrical resistance can therefore be an accurate indicator of the damage state of these interphases, which are sensitive to the oxidizing environment. The global resistance increase presents two distinct phases of evolution in the four tests performed, with a transition around 35-40% of the time to failure. A model is proposed to account for this global resistance change, which proves to be in good agreement with experimental results. Moreover, the evolution of the electrical resistivity during the interposed unload-reload cycles can give key information about the state of the fiber/matrix interfaces which are critical for mechanical properties. Finally, electrical resistance monitoring seems to provide information on the damage state of the material complementary to acoustic emission results, allowing an unprecedented assessment of the evolution of the interphases state during ageing under oxidizing environments.

Keywords: Ceramic Matrix Composites (CMCs); Electrical resistivity; Thermo-mechanical ageing; Oxidizing environment

1. Introduction

SiC/SiC based Ceramic Matrix Composite materials are promising materials for applications in high-temperature jet engines due to their excellent thermo-mechanical properties under oxidizing environments (high strength, toughness and creep resistance) [1-5]. Their introduction in aeronautical engines should enhance the thrust efficiency by reducing weights and increasing the possible service temperatures. The engine parts which are aimed at being made of CMC materials are submitted to highly oxidizing environments, with high temperatures and relatively high pressures of oxidizing species (O₂, H₂O). Yet, it is wellknown that matrix cracking and accompanying debonding and sliding are the main damage modes encountered by these composites, giving access for the oxidizing species to the most critical constituents, fibers and interphases, and hence severely reducing their mechanical properties [6-10]. As CMCs are intended to be used in critical structural parts in the engine, safety is a key concern and the ability to monitor damage accumulation is therefore required.

Most conventional non-destructive evaluation techniques (NDE), such as acousto-ultrasonic, X-ray or thermography, (i) require that the components should be taken out of service for long durations, and (ii) are more efficient for the detection of out-of-plane flaws (such as those leading to delamination) than the typical thin transverse cracks perpendicular to the surface observed in fiber-reinforced composites submitted to in-plane loadings. Acoustic emission (AE) has proved to be an interesting technique for quantifying matrix cracking as well as predicting times to failure [11-13]. However, it cannot be used as an inspection technique at regular time intervals, since damage has to be recorded when it takes place. Moreover, almost no AE activity is recorded during creep tests, which involve crack opening and/or viscoplasticity of one of the constituents (most often the fibers in the case of CMC materials).

The measurement of the change in the electrical resistance of the material (ER) is a particularly promising way of monitoring matrix transverse cracking. This technique has already proved to be pertinent in following the onset and propagation of damage for various materials such as carbon fiber-reinforced polymer composites (CFRP) [14-15], particle reinforced polymer composites [16], and civil engineering materials [17]. CFRP materials have been widely studied, since their electrical resistance is very sensitive to fiber breakage (carbon fibers are a good electrical conductor unlike the polymeric matrix), which is one of the main damage modes in on-axis tension. ER monitoring during room-temperature fatigue tests has been investigated [14, 18], leading for some materials to fatigue life prediction criteria [19]. Recently, the idea of extending the four-probe methods to several pairs of strategically located leads has led to bi-dimensional ER mapping of damage [20], which opens a great field of potential applications. Regarding SiC_f/SiC_m composites, since both the fibers and the matrix are relatively good electrical conductors, their ER has thus proved to be very sensitive to matrix cracking for both CVI (Chemical Vapor Infiltration) and MI (Melt-Infiltration) materials [21], as well as to interlaminar crack growth [22]. High-temperature tests have been monitored using ER measurements with adapted lead locations, which led to the observation that ER increases during creep testing at 1315°C on CVI materials [23]. Further investigations on room-temperature fatigue tests showed that ER increases as well,

displaying a higher rate of increase slightly before failure [24]. All the SiC_f / SiC_m materials tested in the previously mentioned studies were processed with a boron nitride interphase, which is a poor electrical conductor compared to other composite constituents. The SiC_f / [Si-B-C]_m material considered in the present work is the same that in a previous paper focusing on room-temperature damage monitoring and electro-mechanical modeling [25]. This material has a pyrocarbon interphase, which is a high electrical conductor, and should therefore give access to different damage modes.

As previously described, these composites are designed for applications in oxidizing environments, and carbon is known to be very sensitive to oxidation. Hence, it is proposed in the present work to monitor in real time the ER change of $SiC_f / PyC / [Si-B-C]_m$ samples submitted to fatigue and creep tests under oxidizing environments. It should be pointed out that very few studies have been published regarding fatigue tests in oxidizing conditions with real-time ER measurement. Such a study has only been performed on SiC-coated carbon/carbon composites [26], highlighting a strong influence of oxidation-related damages on the ER of the samples. If the damage mechanisms are of course different in a SiC_f / PyC / [Si-B-C]_m composite, this yet tends to confirm that ER could be very sensitive to both mechanical and thermo-chemical related damage in the considered material.

2. Experimental materials and methods

Sustained load tests and cyclic fatigue tests (further referred to as static and cyclic fatigue tests, respectively) have been performed on a Nicalon NL207 SiC fiber-reinforced composite produced by SAFRAN Ceramics referred to as Cerasep® A40C. The fibers were woven in an interlock pattern, with 52% of the fibers orientated in the warp direction and 48% in the weft direction; their total volume fraction is approximately 40%. Prior to the processing of the SiC

matrix, these fibers were coated with a pyrocarbon interphase. The matrix is composed of both ex-polymer SiC (PIP) and CVI layers based on the [Si-B-C] system, with self-healing properties. A self-healing [Si-B-C] seal-coat was finally deposited on the surface of the samples to protect them from oxidizing environments.

Glass fiber-reinforced epoxy tabs were glued on dog-bone shape specimens of a length of 200 mm orientated according to the warp direction, in order to electrically insulate the composite specimens from the testing system. An extensometer (25 mm) with alumina rods was placed on the edge of each specimen. Tests under ambient air were performed on an Instron 8501 machine equipped with a resistive furnace; tests under moist air were performed on another Instron machine (8861, lamp furnace) fitted with a system of environment control, which allows to send a gas flow along the sample placed into a quartz tube.

The selected moist atmosphere is composed of $N_2/O_2/H_2O$: 70/20/10 with a total flow of 110 NL/h (or a gas rate in cold zone of 5 cm/s). A fraction of the oxygen and nitrogen flows through a heated water tank and an automatic system of solenoid valves regulates the percentage of dry gas and wet gas in order to finally have the requested dew point of 46°C (corresponding to 10 kPa of water pressure). This controlled gas mixture is then sent along the sample in the furnace and confined within the quartz tube. Regarding the tests under ambient air, the atmosphere was not controlled but the air humidity content was recorded, showing that the ambient water pressure was 1 kPa with very small variations.

Electrical resistance (ER) was measured using a four-point probe method in order to minimize contact resistance Two types of connection were used to fix the conductive wires to the specimen. Two rings were first painted around the specimen with silver conductive varnish (130 mm apart), in order to collect the surface current on the whole perimeter of the sample (Fig. 1). The inner wires were pasted to these rings using CW2400 conductive epoxy. Shallow

grooves were machined in the edges at the extremities of the sample so that the outer wires could be set in the right place, and then fixed using CW conductive epoxy. This method, similar to the one described in [23], allows the wire to be in contact not only with the seal-coat but also with the inner fibers and interphase.

A constant direct current was applied through the outer wires whereas the associated voltage was measured between the inner wires. A power supply (AOIP PJ6301) provided a current of 10mA, and a voltmeter (Agilent 34970A) measured the induced voltage. Electrical resistance was measured using this system with an accuracy of 0.5 m Ω . The stability of the measure has been checked during 40h once the sample was fixed in the hydraulic jaws and submitted to the selected test temperature (450°C) without any loading being applied.

Acoustic emission signals were additionally recorded, using a MISTRAS Group SA system, equipped with two PICO sensors placed symmetrically on the grips. Data was acquired at a rate of 2 MHz, and the detection threshold was fixed to 50 dB.

Four different tests were performed up to failure, all of them at 450°C and with a maximal stress of 100 MPa applied within the warp direction, on specimens issued from the same production batch. The test temperature of 450°C was chosen because it is critical for the considered material and leads to the shortest lifetimes: the self-healing process is not efficient (the oxidation kinetics of boron-containing phases are too slow), while the oxidation of the carbon interphase is active. Besides, the selected stress and temperature conditions are typical values at which the material would be submitted during service within the considered part. Two of those tests were carried out under ambient air (P(H₂O) \approx 1 kPa): sample SA (Static Ambient) was submitted to sustained loading (i.e. static fatigue), and sample CA (Cyclic Ambient) to cyclic fatigue with a frequency of 1 Hz between 40 MPa and 100 MPa (i.e. R=0.4). The two other tests were performed under moist atmosphere (P(H₂O) = 10 kPa), with

the same mechanical conditions, leading to samples called SM (Static Moist air) and CM (Cyclic Moist air). In order to facilitate comparisons between obtained results, the two types of atmospheres present the same oxygen partial pressure (20 kPa). Characterization unloading-reloading cycles were regularly interposed at a speed of 47MPa/ min. Regarding the cyclic fatigue tests, the fatigue cycles were interrupted at the mid-cycling stress (70 MPa), the sample was then loaded up to 100 MPa, unloaded to 0 MPa, reloaded to 100 MPa, and unloaded down to the stress of 70 MPa at which the fatigue cycles were again performed. Conversely, regarding static fatigue, the sample was simply unloaded from 100 MPa to 0 MPa, and then reloaded back to 100 MPa. The mechanical loading was applied at high temperature, after 4h of stabilization at 450°C.

3. Results

3.1 General observations

Obtained results in terms of lifetimes and percentage of resistance change at failure are summarized in Table 1 for the four different tested samples.

When considering the testing conditions of sample SA, it clearly appears that it was submitted to the less drastic conditions. As a matter of fact, one may point out that: (i) the time to failure is reduced by a factor close to 3 when $P(H_2O)$ is increased from 1 to 10 kPa, for both mechanical conditions and (ii) cyclic fatigue appears to be more severe than static fatigue since the time to failure is divided by 1.5 under ambient air and 1.25 under moist air.

3.2 Global resistance change

The changes in electrical resistivity at failure are significant (up to +213% for sample SM) and very high compared to results previously obtained on the same composite at room

temperature [25]. In this last case, the resistance increased by only 1% at 100 MPa and 42% at failure (occurring at 257 MPa).

All the evolutions in electrical resistivity observed throughout the duration of the tests are plotted on Fig. 2a under a normalized form equal to $\frac{R-R_0}{R_0} \times 100$, where R_0 is the initial zero-load stabilized resistance at 450°C and in the atmosphere of the test, and *R* is the real-time measured resistance under loading.

For the four tests, the resistance increases quite slowly and almost linearly at first, before increasing more quickly, at a starting time which depends on the test conditions. A clear difference appears between the tests performed under a water pressure of 10 kPa and the ones performed under a water pressure of 1 kPa: the resistance increases much quicker with the highest rate of moisture, regardless of the imposed mechanical conditions. Furthermore, taking the SA test as reference (static / 1 kPa H₂O), the change of mechanical conditions from static to cyclic fatigue (CA) slightly increases the resistance change at a given time (as a combination of oxidation and mechanical effects); the change of environmental conditions to 10 kPa of water (SM) has a clearly more pronounced effect, with a rapid and elevated increase in resistance.

Sample CM which has been submitted to cyclic fatigue under moist air presents a surprisingly low increase in relative resistance as compared to sample SM: in the same moist atmosphere, cyclic fatigue leads to a shorter lifetime than creep at the maximum stress, but to a smaller increase in resistance. This observation will be discussed in Section 4.1.

The evolutions of the strain measured at the maximum stress of 100 MPa (Fig. 2b) reveal a higher strain increase for sample SM than for the samples tested in other conditions, similarly to the evolutions of electrical resistance (both plotted as a function of time).

These results are also displayed in another normalized scale on Fig. 3, in terms of the percentage of total resistance increase as a function of. the percentage of sample life (where R_f and t_f stand for the resistance at fracture and the time to fracture, respectively). This graph clearly reveals a transition in the evolution of each sample. The four tests, after an initial transitional period, display a linear phase followed by a stronger nonlinear increase in resistance. Interestingly, it appears that the transition between these two phases occurs at similar percentages of lifetime (35-40%) for the four tests. This observation, not visible on the strain evolutions (Fig. 2b), could be of great interest if one has to quickly estimate the time at failure of a material in given conditions.

3.3 ER evolution during unloading-reloading cycles

In addition to the persistent increase in resistance always observed for all the samples, it can be fruitful to focus on the evolution of the electrical resistance during the interposed quasistatic unloading-reloading cycles, usually aimed at recording the Young's modulus of the studied sample. At the beginning of the tests, as expected, the resistance decreases upon unloading (the cracks are closing and the current has therefore more connections through the material) and it increases again upon reloading (the cracks are re-opening). However, the shape of the stress-resistance cycles rapidly deviates from this "normal" behavior: for sample CM (cyclic fatigue in moist air), after a few hours, the resistance unexpectedly starts to increases during unloading from 100 MPa to 60 MPa before decreasing again until complete unloading (Fig. 4). Conversely, upon reloading, the resistance increases until about 80 MPa, and then decreases between 80 MPa and 100 MPa to almost reach the initial value at which unloading was proceeded (at least for the first 10 to 20 hours of ageing treatment). This point will be explained later. This phenomenon seems to be amplified as the duration of ageing is increased, with a reverse curvature becoming increasingly pronounced. Besides, the hysteretic opening of the upper part (for which the resistance increases) also appears to be increasingly more pronounced.

Conversely, below 40 MPa, the stress-resistance cycles present a regular evolution, with the change in curvature starting just above this level of stress. This should obviously be linked to the cyclic fatigue performed with a R ratio of 0.4, i.e. between 40 MPa and 100 MPa, which is precisely the range of stress for which the resistance displays an unexpected behavior. Indeed, the quasi-static unloading-reloading cycles between 0 and 100 MPa are interposed among fatigue cycles (1 Hz) between 40 and 100 MPa, which means the sample is most of the time not in the stress regime below 40 MPa. This will be further discussed in Section 4.2.

The other test performed under the same conditions, but in ambient air (sample CA), presents a similar behavior (Fig. 5). The evolution of resistance below 40 MPa is very regular whereas, above this value, a reverse curvature is also exhibited, becoming increasingly pronounced. After 200h or more of ageing treatment, the value reached once the characterization cycle has been completed becomes increasingly higher than it was initially. The stresses at which the maxima of resistance are reached are almost independent of the duration of ageing: about 55-60 MPa during unloading, and 80-85 MPa during reloading. It should be noted that this reverse curvature phenomenon is absolutely not visible on the stress-strain loops (Fig. 5b).

Regarding static fatigue, one may observe a different behavior during the characterization cycles for the two tests which were performed (cf. Fig. 6 with the example of sample SA). At 60h, the resistance evolves regularly with a similar behavior during unloading and reloading but, starting from 150h, it exhibits a higher value than the one it had before the cycle was interposed. If, upon reloading, the resistance always increases monotonously, conversely, during unloading at 250h, it remains constant until about 60 MPa but then decreases while the reloading phase still displays a regular increase. The resistance then tends to increase more

and more upon unloading up to 550h where it increases monotonously during unloading as well as during reloading. The stress-strain hysteretic loops (Fig. 6b) present a classical shape, though with a maximum strain reached after reloading being lower than the one before unloading. This has to be linked with the mentioned higher resistance value after the cycle.

Sample SM exhibits the same type of behavior than sample SA, but with an alteration in reversibility reached after shorter durations (the state presented at 250h for sample SA on Fig. 6 is reached at 100h for sample SM).

It can then be clearly inferred that the phenomenon of reverse curvature presented on Fig. 4 and Fig. 5 is linked to cyclic fatigue conditions. Further interpretations will also be detailed in the Section 4.2.

4. Discussion

4.1 Global resistance increase

As already mentioned, the changes in resistance at failure are significantly higher than with previous results obtained on the same composite tested in tension at room temperature [25].

Yet, in this later case, the final crack density was certainly greater than during the fatigue tests performed in the present study with a maximum stress of 100 MPa (respectively, during fatigue tests, the absolute energy of acoustic emission remains at a much lower level, around maximum 40% of that to the ultimate tensile stress). Thereby, the fact that this higher crack density led to smaller increases in resistance means that other mechanisms contribute to the observed resistance changes.

Since it was previously demonstrated that in the considered Cerasep® A40C composite, the pyrocarbon interphase is the main current conductor [25], with a resistivity lower by two

orders of magnitude as compared to the other constituents (fibers, and [Si-B-C]-CVI matrix) taking into account their representative content in the composite, a change in the global resistance of the material has to be related to an alteration the carbon interphase. This alteration has been previously linked to damaging phenomena, i.e. matrix microcracking and related debonding and sliding. Hence, one has to evoke damaging phenomena specifically taking place during cyclic tests and long time exposure to oxidizing environments such as mechanical wear on one hand and oxidation on the other hand.

Indeed, during cyclic fatigue tests, at each unload/reload cycle, the friction between the various interfaces (matrix/interphase, interphase/fiber, between interphase carbon planes) can damage the organization of the pyrocarbon planes within the interphase, and therefore lead to the increase of their resistivity. Moreover, when the cracks reach the fiber tows, they can become paths for oxidizing species leading to a progressive consumption of the carbon interphases, which in turn increases the global resistance of the sample.

This last mechanism appears to be predominant since the two tests performed under a moist atmosphere (10 kPa of water, 20 kPa of O_2 is maintained) and therefore more oxidizing environment have led to quicker and greater increases in resistance after a same duration of fatigue exposure (Fig. 2a). The oxidizing species in a large excess may be less consumed by oxidation close to the sample surface and hence diffuse deeper inside the material bulk. This can be confirmed by the SEM observation of the fracture surface of sample SA (Fig. 7), on which the interphases have completely disappeared because of oxidation (a gap which is not present on the pristine material is visible between fiber and matrix). During static tests, the times before failure are greater than for cyclic fatigue tests, and the cracks are more open, so the oxidation of the interphases is made easier. Indeed, the increases in resistance at failure are much higher for static tests than for fatigue tests.

Taking, as already mentioned, the static test performed under ambient air as a reference test, a change in the environment (from 1 to 10 kPa of water pressure, i.e. from SA to SM) has a greater influence than a change in the mechanical conditions (from static fatigue to cyclic fatigue, i.e. from SA to CA). The cyclic CA test presents a slightly higher increase in resistance compared to the static SA test, which can be related to a supplementary damage due to mechanical wear in addition to the one due to oxidation. However, regarding the tests performed under a controlled moist atmosphere, the static test presents a higher ER increase than the cyclic test. This could mean that for low levels of moisture (i.e. 1 kPa), the mechanical conditions have a predominant influence on the damage of the electrical contacts within the material (typically linked to the pyrocarbon interphase). Conversely, for higher levels of moisture (i.e. 10 kPa), the impediment of electrical conductivity is mostly due to the atmosphere (oxidation of pyrocarbon): under static fatigue, the oxidizing species have an easier access to the bulk of the material, which leads to a faster increase of the electrical resistance.

Figure 3 shows that the global resistance changes of the four tests present first a phase of linear evolution until 35-40% of the time to failure, followed by a phase of nonlinear increase at a higher rate. This must result from a modification and/or an evolution of the main damage mode during the fatigue test, allowing the access of oxidizing species deeper inside the bulk material [27-28]. Indeed, it has been shown that, already for a single crack, once the oxidation of the matrix constituents close to the surface takes place, the quantity of diffusing oxygen toward the interphase increases. This acceleration of oxygen diffusion is enhanced with the increase of the partial pressure of the oxidizing species and the opening of the crack.

A tensile test interrupted at 100 MPa has been performed on the studied material. The polished cross-sections showed that there were cracks in the seal-coat and in the inter-tow matrix, but no crack was reaching the longitudinal fiber tows. Therefore, since the cracks do

not reach the fiber tows at the beginning of the fatigue tests, the oxidizing species do not reach the interphase of the longitudinal fibers which mainly carry the current. The slow linear increase in ER at the beginning of the tests could hence be linked to both mechanical wear in the interphases and oxidation of small amounts of carbon present in the seal-coat. Then, after an ageing duration depending on the test conditions, the cracks propagate enough to reach the longitudinal fiber tows, giving access to the oxidizing species towards the interphases of the longitudinal fibers, and therefore increasing the rate of change of the ER signal. The transition between these two phases seems to occur around 35 to 40% of the time to failure for the four different testing conditions. As this transition can be directly determined during the test (by setting a given percentage of deviation from the linear evolution), this could be a rather easy way to have an estimation of the time to failure at about 40% of the test duration.

Therefore, the measurement of the electrical resistance of the material can provide a real-time monitoring of the damage state of the interphases, which are the key constituent regarding the mechanical properties of the composite [29].

4.2 ER evolution during unloading-reloading cycles

As detailed in section 3.3, the electrical resistance tends to have a non-monotonic evolution during the unloading-reloading cycles interposed under quasi-static conditions. A phenomenon of reverse curvature is observed after a few hours during all the cyclic fatigue tests, with a maximum resistance reached at a non-maximum stress for both unloading and reloading phases (Fig. 4). The maximum resistance is always reached at about the same level of stress for cycles performed at various times, i.e. around 60 MPa during unloading and around 80 MPa during reloading. Moreover, the resistance values below 40 MPa seem unaffected by this reverse curvature and display a regular monotonic evolution. Therefore, the stress conditions of the cyclic fatigue (R=0.4 between 40 and 100 MPa with a mid-stress

of 70 MPa) appear to have a significant influence on the ER evolution during the cycles. At stresses which are not reached during the cyclic fatigue, the ER evolution is unaffected: the debonded fiber/matrix interface is submitted to sliding along its whole length whereas sliding only occurs along a shorter length, around the matrix crack, during cyclic fatigue. One may think that only a fraction of the debonded interfaces generated by the initial loading at 100 MPa are then submitted to mechanical wear and oxidation. Shortly after reaching the mid-stress value of 70 MPa (i.e. slightly under this value for unloading and slightly above for reloading), the resistance reaches its maximum level. A scenario can be proposed to explain these correlations (Fig. 8): if, during cyclic fatigue, mechanical wear affects a fraction of the various interfaces of the composites (fiber/interphase, interphase/matrix, intra-interphase) then, the softest part can be worn out between the positions related to minimum and maximum stress (i.e. between 40 and 100 MPa).

Hence, at the intermediate position of 70 MPa, the hardest part stands at the middle of the generated cavity, with a loss of electrical contacts and therefore an increased resistance. When the stress reaches the lowest value of 40 MPa the extremities of the generated cavity are again connected, which decreases the resistance. Between 40 MPa and zero load, i.e. once connections have been recovered, crack closure accounts for the regular decrease in ER. During reloading, the resistance is maximum when the middle position with minimum contacts is reached, at a stress slightly above 70 MPa because of friction. Then, getting closer to 100 MPa, electrical contacts are formed again, and the resistance decreases. The maximum ER is reached for different stress levels during unloading and reloading because of friction and hysteresis effects: the same relative position within the interfaces is reached slightly under 70 MPa during unloading and slightly above 70 MPa during reloading.

This mechanism being qualitatively described, it is then possible to define indicators in order to have a more quantitative analysis. Indeed, the shape of these stress-resistance cycles and the amplitude of the reverse curvatures evolve during the ageing of the samples. Several indicators can be analyzed, such as the "resistive modulus", defined as the stress/resistance slope at low levels of stresses, by analogy with the mechanical modulus. Initially very high (because of the low dependence of ER on stress), it quickly drops, as the application of the same stress leads to higher resistance increases. It is proposed to focus on the difference between the maximum resistance (reached during either unloading and reloading) and the residual resistance at zero stress, therefore defining two indicators I_{unload} and I_{reload} (Fig. 9a and 9b).

These indicators may be linked to a "resistive modulus" (or more precisely the inverse of a modulus) introduced by analogy with the mechanical Young's modulus, since the maxima in resistance are always more or less reached at the same stress (they are related to the slope of the Stress-Resistance curve). I_{unload} and I_{reload} can be evaluated for each time at which a characterization unloading-reloading cycle was performed and their evolution as a function of time is plotted in Fig. 9c for sample CM and in Fig. 9d for sample CA. For these two tests, the curves thus obtained follow a surprisingly similar pattern with three phases: initial increase, steady state phase, final increase. At the beginning of the tests, I_{unload} and I_{reload} have low values in relation with the level of damage in the material which is also low: the resistance is almost not modified between 0 and 100 MPa. Then with the increasing level of damage (development of matrix cracking, debond lengths and cracks opening), the resistance of the sample becomes more sensitive to the applied stress. These three phases of evolution could be compared to creep behavior, with an initial transitory phase, a steady evolution and, finally, an acceleration of damage.

The times of transition between phases are very different for the two tests (20h-60h for CM, 60h-200h for CA), but it is really worth mentioning that the percentages of time to failure are very close, i.e. around 15% for phase 1 to phase 2 and around 50% for phase 2 to phase 3.

Hence, it appears that the increase in water pressure (the only different condition between the two tests) has accelerated the damage of the sample in terms of resistive modulus, but the mechanisms involved have not been modified. Such a consistent evolution of resistive modulus could be of great interest for life prediction if a transition could be accurately identified as soon as 15% of the time to failure

Regarding static fatigue tests, no reverse curvature has been ever observed with the ER evolutions upon reloading (Fig. 6), which supports the assumption that this phenomenon closely linked to cyclic loading. The evolution of the shape of the cycles displayed in Fig. 6 can be explained as follows: between each characterization cycle, performed every 50h after 100h of ageing, the sample is then left with the same applied stress without any disruption during these 50 hours. It can therefore stabilize in this steady state during which it undergoes micro-electrical contacts linked to micro-welding helped by the fluid oxide generated by the self-healing matrix at 450°C. During unloading, these micro-contacts are broken, which tends to increase the resistance whereas, during reloading, they are not generated again because this is a time-dependant process (hence the ER increases as well). This mechanism is amplified with the level of damage of the material.

The analysis of the evolution of ER during unloading-reloading cycles can provide significant information regarding mechanisms occurring inside the bulk of the material, within micro-interfaces. The interpretations described here still need further confirmation by tests performed in different conditions, yet these indicators could have a high potential regarding life prediction.

4.3 Modeling approach for the global resistance evolution

The global evolution of ER during the four fatigue tests seems to be ruled by the same mechanisms (similar phases of evolution), with time and magnitude factors depending on the

test conditions. It therefore appears possible to build a model which would quantitatively estimate the change in ER evolution induced by a change of testing conditions, especially regarding the water pressure which was proved to greatly influence the global ER evolution. For more clarity, all the following equations involve resistance instead of specific resistance, which does not constitute a drawback in the present study since the tested samples all present the same geometry. However, the model can be easily adapted to specific resistances if one wishes to apply it to samples of various geometries.

As demonstrated in [25], the change in ER in the Cerasep® A40C composite can be described by the following equation:

$$\frac{\Delta R(\varepsilon)}{R_0} = (1 + \alpha \varepsilon) [K L_d(\varepsilon) \rho_c(\varepsilon) + 1] - 1$$
(1)

In Eq. 1, $\Delta R(\varepsilon) = R(\varepsilon) - R_0$ is the difference between the electrical resistance measured at strain ε and the initial resistance R_0 (which is the stabilized resistance at the test temperature for high temperature tests), L_d is the debond density (sum of all debonded lengths of the sample), ρ_c is the transverse matrix crack density, α and K are two coefficients to be determined (respectively linked to the piezo-resistance factor of pyrocarbon and to the damage related increase in resistivity).

During the fatigue tests of this study with a maximal stress of 100 MPa, the strains are relatively low (maximum strain around 0.3%). Hence, Eq. 2 can be considered as a first order approximation, where *A* is a coefficient of proportionality.

$$\frac{\Delta R(\varepsilon)}{R_0} = A L_d(\varepsilon) \rho_c(\varepsilon)$$
⁽²⁾

It has been shown that the transverse matrix crack density is directly related to the cumulative energy of the acoustic emission signal [30-31]. This energy, recorded during the two static tests (SA and SM), appeared to be almost constant from 3 to 5 hours after the beginning of the

test up to the failure of the specimen. Hence, it can be assumed that the transverse matrix crack density remains constant after the initial damage of the specimen (i.e. only debonding is aimed at progressing). Equation (2) can then also be written again as follows, with A' another coefficient of proportionality:

$$\frac{\Delta R(\varepsilon)}{R_0} = A' L_d(\varepsilon) \tag{3}$$

With these assumptions at hand, the increase in resistance then appears to be directly proportional to an increase in the debond density.

As described in 4.1, it is assumed that after a phase of linear increase in ER linked to the development of the micro-crack network generated within the seal-coat, the micro-cracks start to develop within the fiber tows. From that moment, the oxidizing species present in the environment have an access to the pyrocarbon interphase deposited on the fibers, which is very sensitive to oxidation. As the transverse matrix crack density is assumed to be constant (no increase in acoustic energy), the crack does not propagate within the tow, and the progression of degradation of the interphase is mainly ruled by oxidation mechanisms. When considering a transverse cross-section within the plane (y,z) (i.e. the plane of the microcracks), it appears that the oxidizing species would first attack the fibers closest to the sealcoat (Fig. 10). Oxidation then progresses (i) towards the bulk of the material and the next rank of fibers, from an interphase to another close interphase (z direction) and (ii) along the same longitudinal fibers following the damaged interphase (x longitudinal direction). As the oxidation of carbon is active, with the formation of CO₂ gas, the kinetics of the reaction can be considered as linear (no passivation layer is generated and the diffusion limitation of O₂ may be considered as negligible through the narrow opened pathway by oxidation since the oxidation kinetic rate (or quantity of O₂ consumed as a function of time) is very slow at such a low temperature). In a first approximation, a simple incremental modeling is thus proposed to explain the observed ER evolutions as a function of the environmental conditions. Therefore, for a single longitudinal fiber cut by a crack, the debond length l_d can be expressed by Eq. 4, with a linear kinetic rate k.

$$l_d(t) = kt \tag{4}$$

Similarly, always assuming an active oxidation with generation of gas, the time required to oxidize the next rank of fiber towards the bulk of the material in the Z direction can be considered as constant (t_{ox}). This duration depends on k and on a characteristic distance l_0 which is an average distance between two ranks of fibers:

$$t_{ox} = l_0/k \tag{5}$$

Hence, the progression of oxidation can be schematized as depicted in Fig. 10. The initial time t=0 is taken when the oxidizing species first reach the closest fibers. After t_{ox} , the first rank of fibers is oxidized ($l_d = kt_{ox}$ for each of these fibers) which leads to a global debond density (sum of all debond lengths) of $L_d(t_{ox}) = N k t_{ox}$ (as there are N fibers in a rank). After 2 t_{ox} , the second rank is oxidized as well; meanwhile, the interphases along the longitudinal fibers of the first rank have been attacked. Each of the fiber reached by the oxidizing species, whatever its rank, has developed a debond length $\Delta l_d = kt_{ox}$ during an additional duration t_{ox} (between $t = t_{ox}$ and $t = 2t_{ox}$) which leads to a global debond density of $L_d(2t_{ox}) = 3N k t_{ox}$. Next, at $t = 3 t_{ox}$, the third rank is oxidized, the second rank fibers have a debond length of $l_d = 2kt_{ox}$ and the first rank fibers are debonded over $l_d = 3kt_{ox}$ since they have been submitted to oxidation during a duration of $3t_{ox}$. The global debond density hence increases to $L_d(3t_{ox}) = (3 + 2 + 1)N k t_{ox}$. Similarly, at $t = n t_{ox}$, the nth rank of fibers is oxidized and the debond density reaches the value expressed in Eq. 6.

$$L_d(nt_{ox}) = (n + \dots + 3 + 2 + 1)N \ k \ t_{ox} = \frac{n(n+1)}{2} \ N \ k \ t_{ox}$$
(6)

Introducing the change of variable $t = nt_{ox}$, Eq. 6 can easily be turned into Eq 7 as follows:

$$L_d(t) = \frac{Nk}{2t_{ox}}t(t+t_{ox})$$
⁽⁷⁾

In order to assess the influence of the pressure of oxidizing species on L_d , the linear kinetic rate k can be expressed as a function of oxygen and water pressures, and their associated orders :

$$k = k_0 P (H_2 0)^m P (O_2)^p$$
(8)

The combination of Eqs. 5, 7 and 8 can lead to a new formulation of L_d :

$$L_d(t) = \frac{Nk_0^2}{2l_0} P(H_2 O)^{2m} P(O_2)^{2p} t (t + t_{ox})$$
(9)

This theoretical approach can now be compared to the experimental observations. First, the polished transverse cross-section of sample SM (static fatigue, moist air) presented in Fig. 11 is in close agreement with the mechanism schematically depicted in Fig. 10. Indeed, the fibers closest to the surface are heavily oxidized, and the damaged zones progress towards the bulk of the material over around four fiber tows.

Moreover, in order to assess Eq. 9, the change in ER is plotted in Fig. 12 as a function of the square of the time, and linear regressions are presented for the last part of the evolution, which should be linear according to the model described above. This point is evidenced by the following equation obtained by reporting Eq.9 into Eq.3, revealing a quasi linear behavior as soon as t_{ox} is very small comparatively to t.

$$\frac{\Delta R(t)}{R_0} = A' \frac{Nk_0^2}{2l_0} P(H_2 0)^{2m} P(O_2)^{2p} t(t + t_{ox})$$
(10)

It appears that for three of the four performed test (CM, SA, CA), an excellent linear fit is achieved, which strongly supports the proposed model.

Considering a single micro-crack, it appears from Fig. 10 that the progression of oxidation would be affected by several discontinuities, when reaching a different fiber tow. However, because of the high number of micro-cracks and of the various positions of fiber tows linked to the weaving, this effect is average and does not appear on the overall increase in resistance. The penetration rate of the oxidation front is most likely slightly higher under cyclic fatigue (CA) than under static fatigue (SA) because of a more important wear-related interface degradation.

In order to further assess the model, an analysis of the parabolic coefficient γ given by $L_d(t) = \gamma t^2 + \delta t + \delta'$ can be performed (with γ proportional to $P(H_2O)^{2m} \times P(O_2)^{2p}$). It is proposed to compare the γ coefficients obtained from the tests CA (cyclic, ambient air) and CM (cyclic, moist air) for which the only difference is the water pressure. As P(O_2) is identical for these two tests, Eq.9 gives the following theoretical ratio between the two γ coefficients :

$$\frac{\gamma_{CM}}{\gamma_{CA}} = \frac{P(H_2 O)_{CM}^{2m}}{P(H_2 O)_{CA}^{2m}} = \left(\frac{10 \ kPa}{1 \ kPa}\right)^{2m} = 10^{2m} \tag{10}$$

The reactive order associated to water pressure in the oxidation of carbon has been evaluated to m=0.31 in [32] for similar composites. Hence, a theoretical γ ratio can be estimated:

$$\left(\frac{\gamma_{CM}}{\gamma_{CA}}\right)_{th} = 4.1\tag{11}$$

This ratio can directly be compared to the linear coefficients issuing from the regressions presented in Fig. 12.

$$\left(\frac{\gamma_{CM}}{\gamma_{CA}}\right)_{exp} = \frac{2.82}{0.63} = 4.5$$
 (12)

The estimated theoretical ratio and the experimental one are very close, which strongly supports the theoretical global approach previously described. Regarding the SM test (static fatigue, moist air), the ER increase is actually closer to be depending on t³ rather than t². The parabolic evolution issuing basically from a bidimensional propagation of oxidation, it could be inferred that for sample SM, submitted to the most extreme conditions regarding oxidation (highly moist air with open cracks), the oxidation progresses as well in a third direction (y direction), represented on Fig. 13. With a high increase of the oxidized lengths, a limitation by oxygen diffusion may also be involved in the advance of the oxidation front.

5. Conclusion

Four ageing tests have been performed to failure with a maximum stress of 100 MPa and under various mechanical and environmental conditions: static fatigue (also referred to as creep if viscoplasticity is involved) or cyclic fatigue at 1 Hz, ambient air (1 kPa of water) or moist air (10 kPa of water). The electrical resistance of the samples was continuously recorded during the ageing tests using a four-point probe method. A higher level of moisture in the environment has led to shorter life durations as well as to faster increases in resistance. The following conclusions can be highlighted :

- (i) The increase in ER can be directly linked to damage of the pyrocarbon interphase in the considered composite. ER monitoring can therefore give real-time information on the level of damage of the interphase, which is a key constituent in the mechanical properties of CMCs.
- (ii) The evolution of ER follows a similar pattern for the four different test conditions,with an initial linear phase followed by a phase of increase at a higher rate. For

these four performed tests, the transition between these two phases occurs between 35 and 40% of the time to failure. This observation could have a great potential regarding lifetime estimation.

- (iii) The analysis of the evolution of ER during quasi-static unloading-reloading cycles can give access to phenomena occurring within interfaces situated in the bulk of the material, besides difficult to be reached with other monitoring techniques. The dependence on damage of ER evolution during cycles requires further investigation, but could be of great value as it seems to follow similar sequences with different characteristic times for different test conditions.
- (iv) A theoretical approach has been proposed regarding the evolution of the global increase in resistance. It has been linked to the progression of oxidation from the seal-coat to the bulk in both the longitudinal X direction and through the thickness (Z direction), with a rate depending on the environmental conditions. The model has proved to be in good agreement with experimental data for 3 of the 4 performed tests, and an explanation has been suggested for the fourth one.

Electrical resistance was shown to be a very valuable monitoring technique regarding ageing tests in oxidizing environments. The combinated effects of the mechanical and oxidation damage on the interphase and consequently on the ER should be investigated further, as well as the evolution of ER during the unloading-reloading loops, which seems really promising but not fully understood yet. The study of relationships between electrical resistance evolutions and strain evolutions could also be helpful to point out the effects of mechanical damage sequences on electrical changes in CMCs. Further efforts regarding modeling and an enhanced understanding of the phases of evolution of ER could possibly allow this monitoring technique to be used in industrial applications for lifetime estimations.

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Figures

Figure 1 - Specimen configuration with electrical leads, the tube confining the gas flow and the furnace area.



Figure 2 – (a) Relative electrical resistance change as a function of time for the 4 tests performed at 450° C and (b) evolution of strain (measured at the maximum stress 100 MPa) as a function of time for the same 4 tests.



Figure 3 - Resistance change in terms of the percentage of total resistance increase as a function of the percentage of sample life for the 4 tests performed at 450° C.



Figure 4 - Changes in resistance observed at the beginning of the test upon interposed unloading-reloading cycles after various durations of ageing (sample CM, cyclic fatigue at 1 Hz, humid air: $P(H_2O) \approx 10$ kPa).



Figure 5- (a) Resistance as a function of stress and (b) stress as a function of time during unloading - reloading cycles after various durations of ageing (sample CA, cyclic fatigue, ambient air: $P(H_2O) \approx 1$ kPa).



Figure 6 – (a) Resistance as a function of stress and (b) stress as a function of time during unloading - reloading cycles after various durations of ageing (sample SA, static fatigue, ambient air: $P(H_2O) \approx 1$ kPa).



Figure 7 - SEM image of the break surface and absence of interphase between fiber and matrix for sample SA.



Figure 8 - Schematic representation of the fiber/matrix interfaces for various stresses, and link with the measured resistance at these stresses.



Figure 9 - (a) Definition of R_{res} and R_{max} for unloading and reloading phases on the cycle performed after 100h during test CA, (b) Definition of the indicators I_{unload} and I_{reload} , (c) evolution of I_{unload} and I_{reload} during test CM, (d) evolution of I_{unload} and I_{reload} during test CA.



Figure 10 – Schematic evolution of the transverse cross-section in the plane of a micro-crack (Dark zones on fibers are zones where the interphase is oxidized).



Figure 11- Micrography of a transverse cross-section of sample SM (bottom edge: surface of the sample).



Figure 12 – Evolution of ER as a function of the square of time for four ageing tests, and related linear regressions.



Figure 13 - Schematic representation of the progression of oxidation in a third direction (y direction) adapted to sample SM.



Table 1 - Name, time at failure and resistance change at failure for the four tested samples according to the mechanical and environmental conditions (at atmospheric pressure with a constant partial pressure of oxygen 20 kPa) to which they were submitted

		$P(H_2O) \approx 1 \text{ kPa}$	$P(H_2O) = 10 \text{ kPa}$
Static fatigue	Sample name	SA	SM
	Time at failure	570 h	160 h
	Resistance change at failure	+153%	+213%
Cyclic fatigue (1 Hz)	Sample name	CA	СМ
	Time at failure	373 h	129 h
	Resistance change at failure	+ 79%	+ 42%